

Mathematics 54 First Long Exam M54\_LE1\_005 Elementary Analysis II First Semester, AY 2013-2014

I. Do the integration.

1. 
$$\int \tan^5 x \sec^3 x \, dx$$
  
2.  $\int \frac{dx}{x^2 \sqrt{4 - x^2}}$   
3.  $\int \frac{dx}{x^3 - x^2}$   
4.  $\int \sin x \sinh x \, dx$   
5.  $\int_{-\infty}^{\frac{3}{2}} \frac{dx}{4x^2 + 9}$   
6.  $\int_{0}^{\frac{\pi}{6}} \frac{\cos x \, dx}{\sqrt{1 - 2\sin x}}$ 

- II. A bacterial culture growing exponentially increases from 10 grams to 50 grams in the period from 7 AM to 9 AM. How many grams of bacteria is present at noon of the same day?
- III. A curve passes through the point (1,2) and is orthogonal to every member of the family of curves  $y^2 = kx$ ,  $k \in \mathbb{R}$ . Determine the equation of the curve.

## END Total: 40 points