# UPSCHOOLOF STATISTICSSTUDENTCOUNCIL <br>  

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Mathematics 17
Fifth Long Examination

College Algebra and Trigonometry
First Semester, AY 2012-2013
I.

1. Write TRUE if the statement is true, otherwise, write FALSE.

1 point each
(a) Given any right triangle, the angle opposite the hypotenuse has the largest measure.
(b) If $r, \theta \in \mathbb{R}$, then $r \operatorname{cis}(-\theta)=-r c i s \theta$.
2. Evaluate the following

2 points each
(a) $\cot ^{-1}\left(\cot \left(\frac{13 \pi}{12}\right)\right)$
(b) $\sin \left(\cos ^{-1}\left(\frac{1}{2}\right)\right)$
II.

1. Evaluate: $\sin \left(\csc ^{-1}(2)-\sin ^{-1}\left(-\frac{3}{5}\right)\right)$

4 points
2. Simplify and express the final answer in rectangular form: $\frac{\left[2 \operatorname{cis}\left(53^{\circ}\right)\right]^{5}}{16 \operatorname{cis}\left(-65^{\circ}\right) \operatorname{cis}\left(90^{\circ}\right)} \quad 4$ points
III.

1. Solve for $x: \operatorname{Arcsec}(x+2)+\operatorname{Arctan}(-\sqrt{3})-3 \operatorname{Arccos} 1=0$

4 points
2. Solve for all complex values of $z$ (express $z$ in standard polar form): $z^{3}=\sqrt{2}-\sqrt{2} i \quad 4$ points
IV.

1. Officer Stewie Griffin (OS) is on top of a lighthouse when he sees Prisoner Bryan (PB) at an angle of depression of $45^{\circ}$ trying to escape by rowing a boat away from the lighthouse. After an hour, PB is now 4 miles away from OS at an angle of depression of $15^{\circ}$. How far has PB rowed at that time?
2. From her house, Dora decided to go trick-or-treating in Willy Wonka's Chocolate Factory. The Map told Dora that she must first travel 8 km from her house to Count Dracula's Hotel Transylvania in the direction $\mathrm{S} 76^{\circ} \mathrm{E}$; and then 5 km more from the hotel in the direction $\mathrm{S} 44^{\circ} \mathrm{W}$ to reach the factory. How far is her house from the hotel?
